

Learning Math by Teaching Math: A Case Study in Intelligent Tutoring and Educational Data Mining

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A word of thanks



Matsuda



Koedinger



Keiser



Yarzebinski



Ong



Bringula



Dela Cruz



Basa



Let's talk about you

- What are your usual teaching strategies for learning math?
- What are the usual assessment strategies?
- How do your teachers process the assessment data?



Context

- How can we use computers for mathematics education



The usual suspects

- Drills
- Educational games



Less usual, less common suspects

- Intelligent tutoring systems



What are ITSs?

- Computer-based learning environments that use artificial intelligence to provide the learner with customized feedback and guidance



Outline

- Introduction to SimStudent
- Data collection methods
- SimStudent findings
 - Effectiveness of learning by teaching
 - Self-explanation
 - Prior learning and other factors



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Learning by Teaching

- A well-known effective learning strategy
 - Across ages, domains, structures, etc...
- Cognitive and social theories have yet to be investigated
 - When and how students learn by teaching?



Solution: Teachable Agent

- Pedagogical agent that students can teach
- Does the TA work as a peer for students to learn by teaching?
- Do we need a genuine machine learning technology?
 - What is it the ML brings us that would otherwise impractical?



SimStudent: a teachable agent

- Learns cognitive skills from tutored-problem solving
- Programming by demonstration
 - Production model
 - Hybrid learning for what, when, and how to apply a skill
 - Version space
 - Inductive logic programming
 - Iterative-deepening search



Tutoring Stacy

- Try tutoring Stacy to solve problems such as
 - $3x = 6$
 - $2x + 1 = 5$
 - $5x + 3 = 6x - 2$
- Try tutoring the WRONG rules and see what happens



SimStudent models human learning

- It is possible for SimStudent to learn the wrong thing



Example: Learning to subtract a constant term

First example

LHS	RHS	Skill Operand
3x+1	= x+4	subtract 1
	=	

I see $3x$, 1 , x , and 4 in the equation. I wonder where the '1' came from.

Learning to subtract a constant number

Subtract the difference between 4 and 3...

Subtract the coefficient of X ...

Subtract the last term on the left-hand side...



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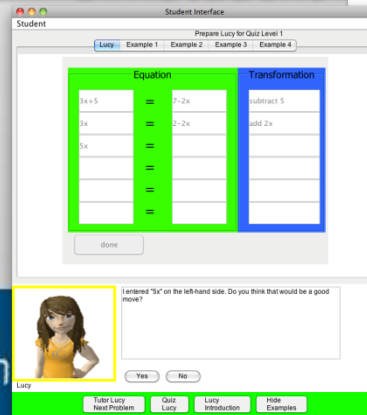
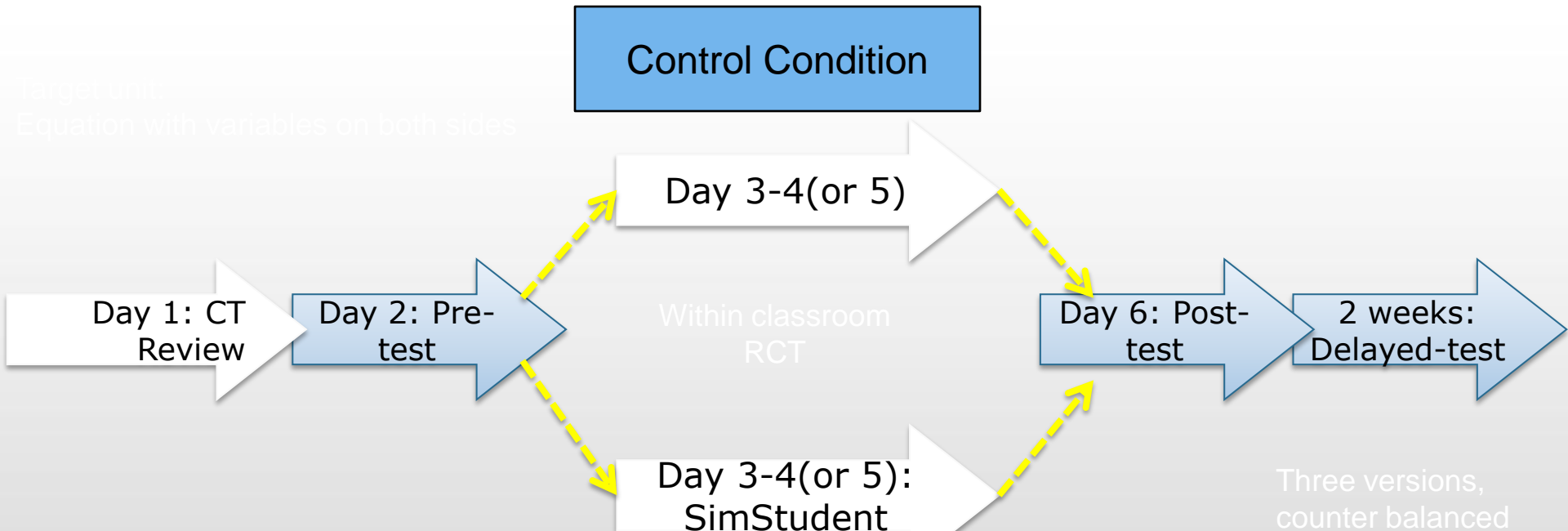


Outline

- Introduction to SimStudent
- **Data collection methods**
- SimStudent findings
 - Shallow learning
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 - Prior learning and other factors



Structure of the Study



Pre, post, and delayed post

- Isomorphic
- Counterbalanced
- Divided into procedural and conceptual parts
- Only the procedural results were used to measure gains



Process data

- Problems tutored
- Feedback provided
- Steps performed
- Examples reviewed
- Hints requested
- Quiz attempts



Data collection venues

- Pittsburgh, PA
- University of the East, Manila



Outline

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What do you think?

- Is learning by teaching effective?
- Will the students using SimStudent learn more than those in the control condition?

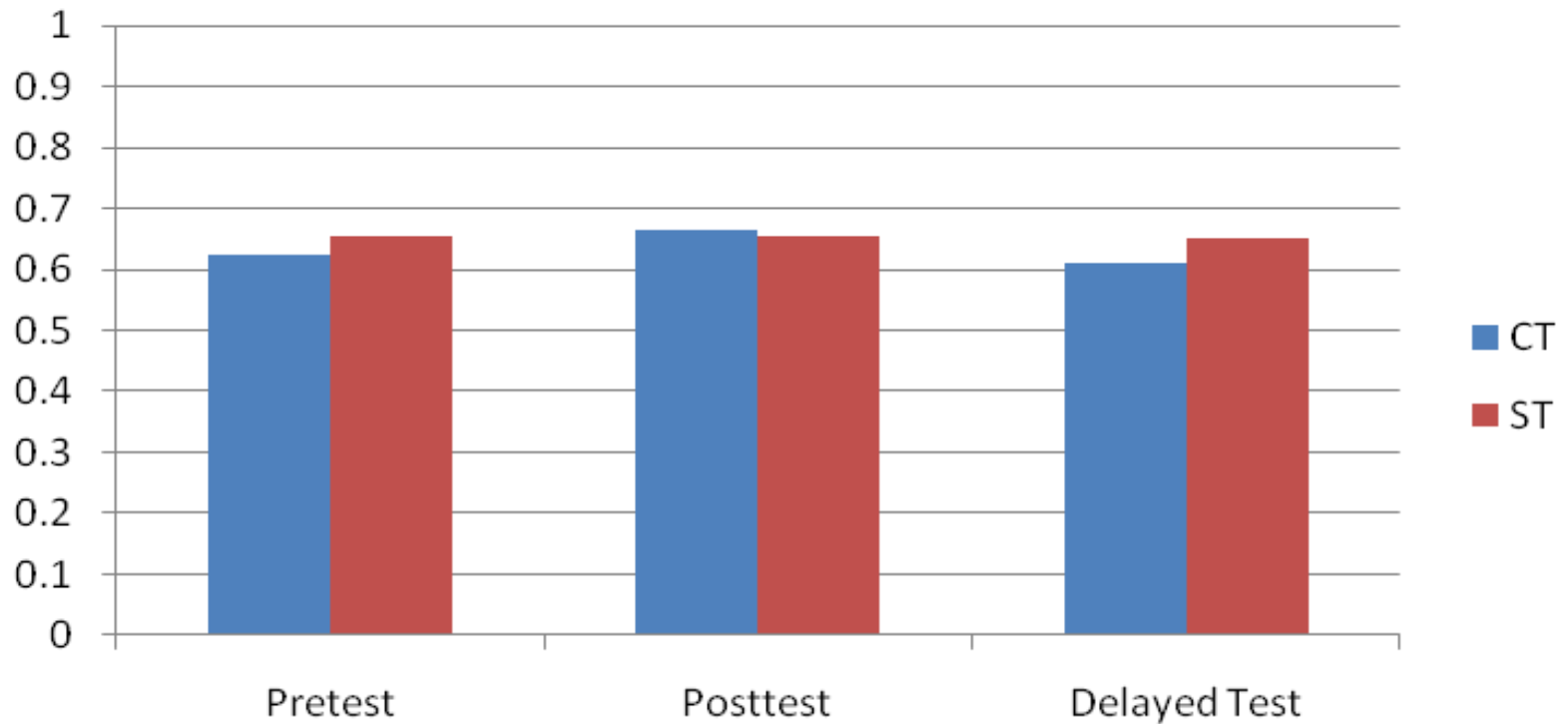


And the results are...



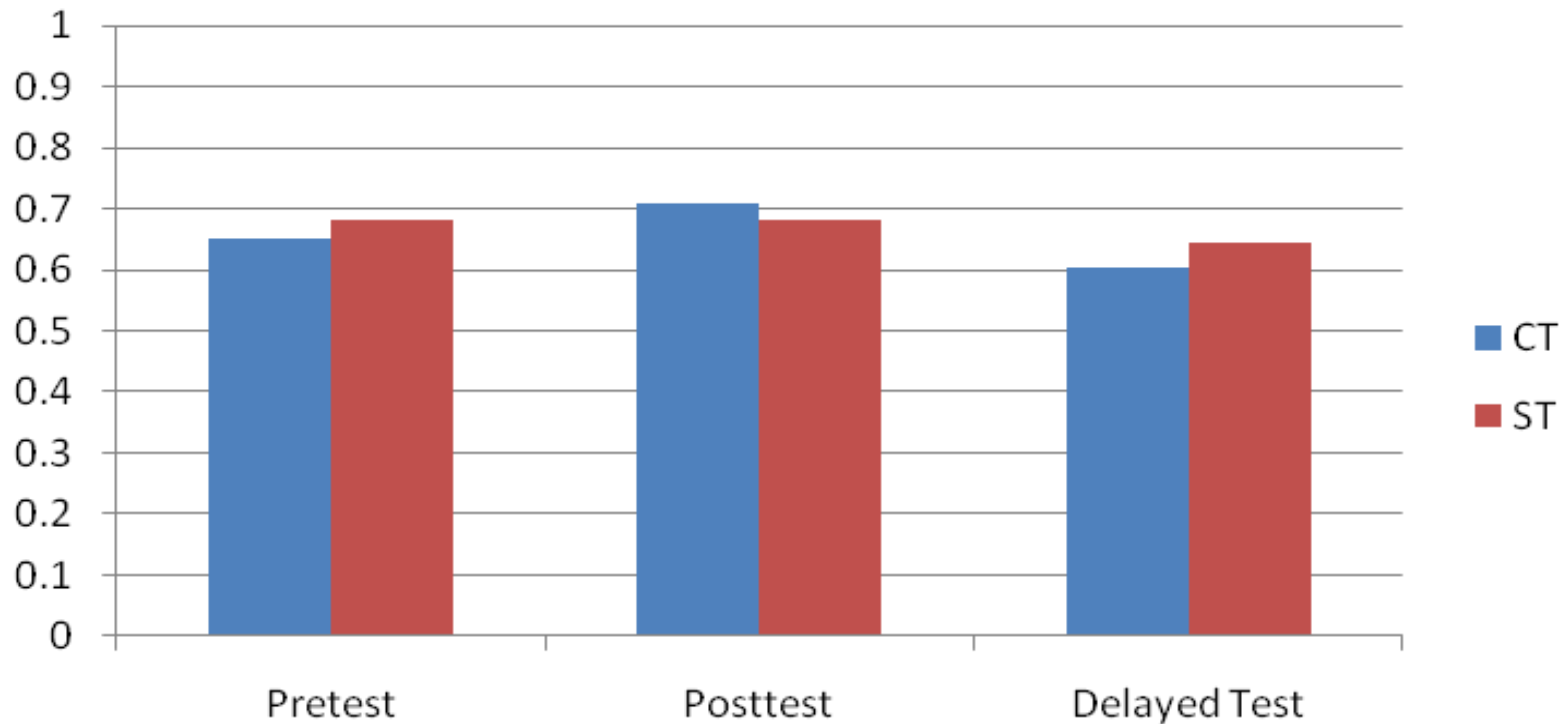
Overall Test Scores

N=74



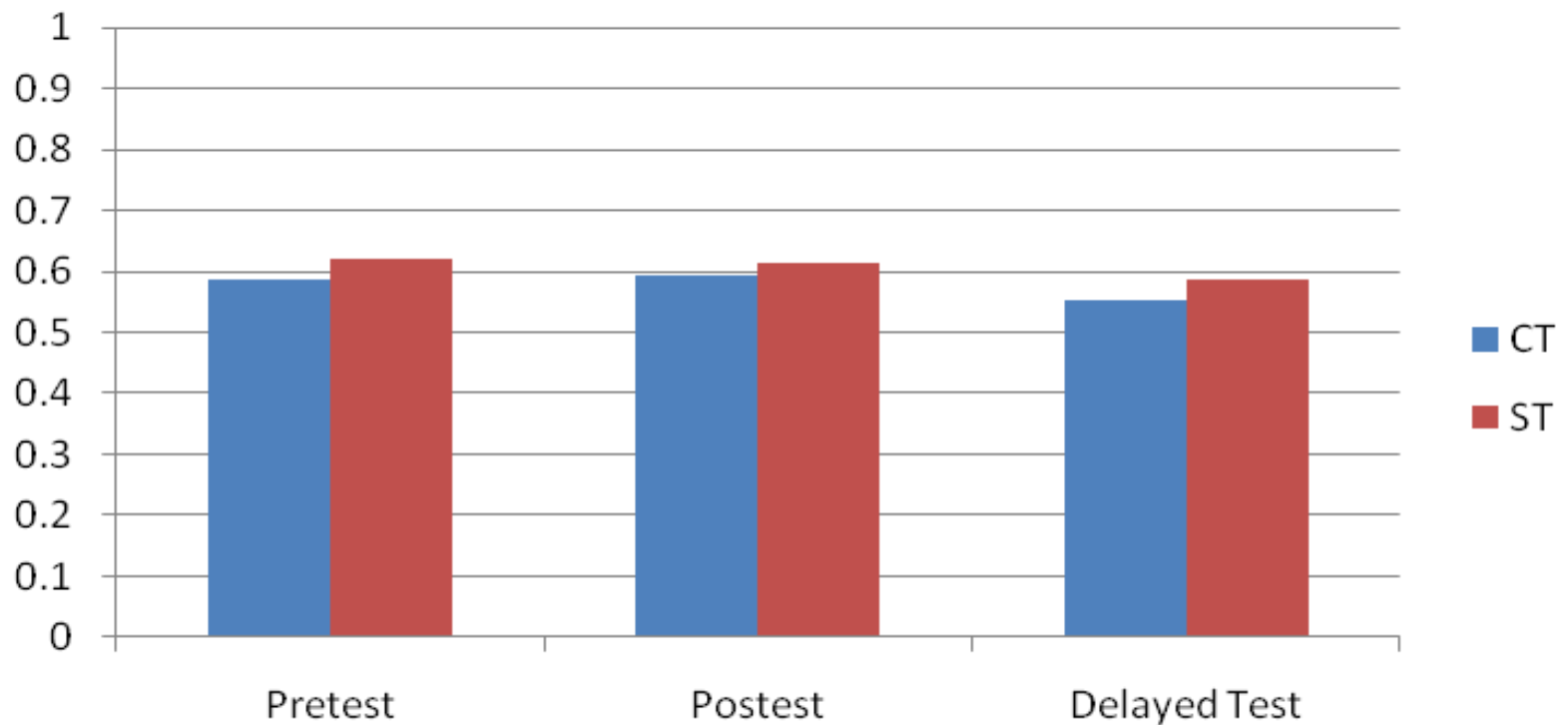
Procedural Items

N=74



Conceptual Items

N=74



In brief

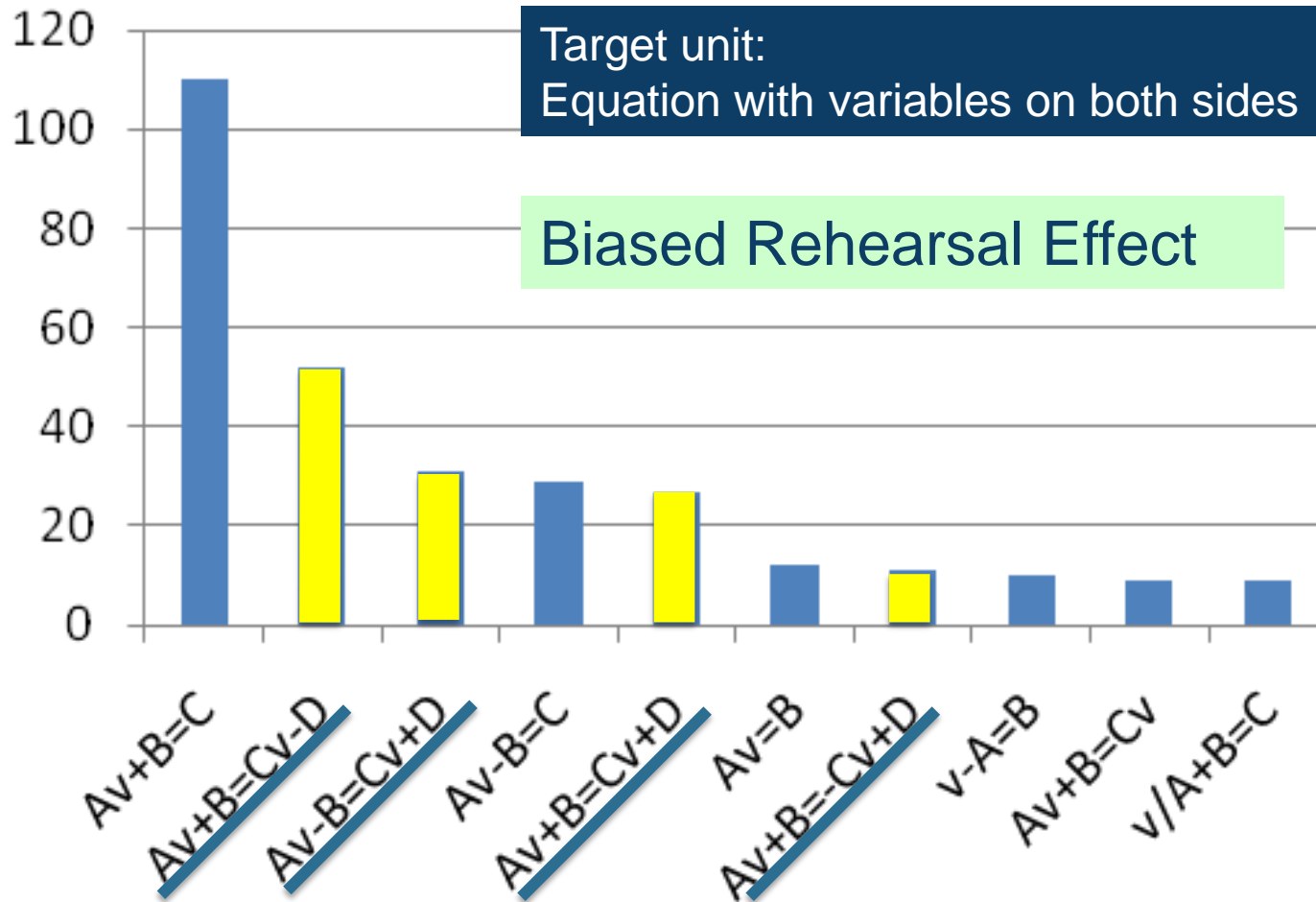
- No significant learning gains with SimStudent
- Students with weak prior knowledge learned more from the control condition



Why???



Problems Used for Tutoring



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Self-Explanation Hypothesis

- Self-explanation facilitates learning from examples
- The same effect for such a meta-cognitive reflection might occur for tutor learning
- Prompting students to explain and justify their tutoring activities and decision might facilitate tutor learning



SimStudent asks for explanations

- A **new problem** posed by a student
 - “why should I do this problem?”
- Corrective feedback on an **error**
 - “But I put divide 3 for $3x=9$. Why doesn't divide 2 work now?”
- A step **demonstrated** by the student as a hint
 - “Why did you do such?”



What do you think?

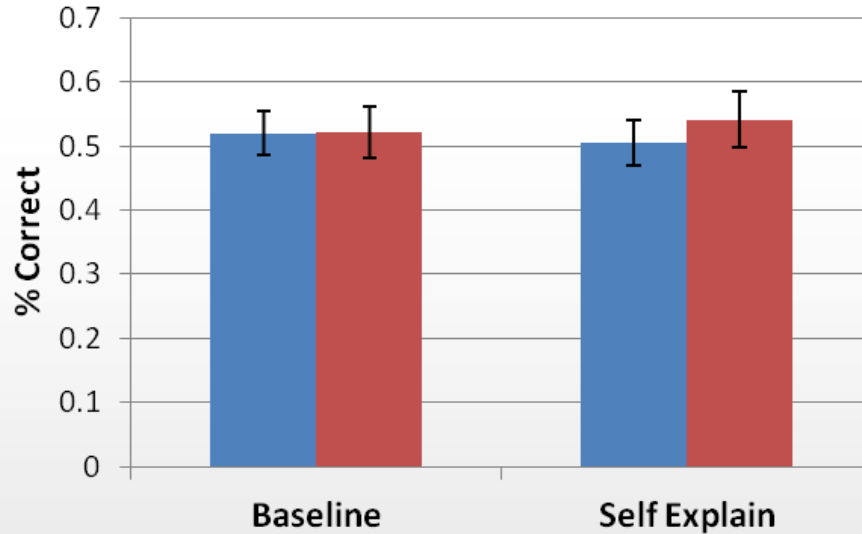
- Is self-explanation effective?
- Will students who self-explain learn more than those who do not?



And the results are...

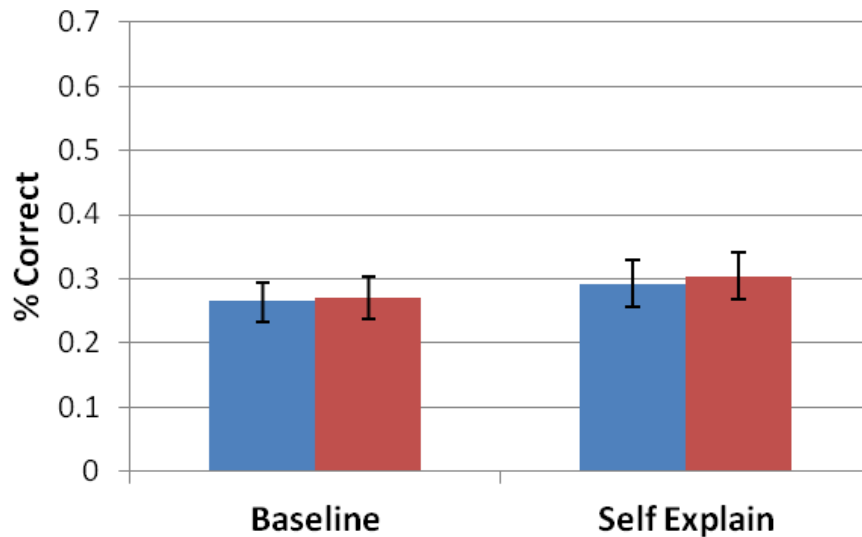


Results: Test Scores



Procedural Skill Test

■ Pretest
■ Posttest



Conceptual Knowledge Test

■ Pretest
■ Posttest



Self-Explanation Effect for Tutor Learning

- Regression analysis
 - Dependent variable
 - Normalized gain for the procedural skill test
 - Independent variables
 - Type of explanation (new problem, error, hint)
 - Format of explanation (dropdown, free input, mix)
 - Degree of elaboration (shallow, elaborated)
 - Frequency of denial (SE skipped / total question asked)
 - Domain specificity (# of math term used)
- No notable effect of self-explanation for tutor learning



In brief

- Overall, the version of APLUS and SimStudent used for the Self-Explanation study showed weak effect on procedural skill acquisition
 - The latest version showed a significant main effect of test (pre vs. post)
- SimStudent did learn skills from students – Quiz passed
 - This was actually shallow learning!
- SE students achieved the same test scores with fewer problems.
- No particular self-explanation effect confirmed
 - System may need to provide constructive feedback for “shallow” explanations



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Prior knowledge

- Pre-test scores are highly predictive of post-test scores.
- Why do some students with low prior knowledge do better than others?
- What other factors affect tutor learning?



US vs PH study

- Pre, post, and delayed post
- SimStudent SE vs baseline



Overall test results

■ PH

- No statistically significant difference between pre and post
 - Statistically significant difference between pre and delayed post
- ## ■ No condition difference in post-test scores in either country
- SEs did not affect tutor learning



Country differences

- US students had higher prior learning
- Did better on the post-test
- Learned more



Within the PH dataset

- Some students in the PH dataset did better than others.
- Their SimStudent passed 2 out of 4 quiz sections (termed “passing Sx students”)
- Why?
- What did they do that was different?



Copying quiz items

- Did passing S1 and S2 students use more quiz items for tutoring?



Copying quiz items

- Did passing S1 and S2 students use more quiz items for tutoring?

- No.
 - No notable difference in number of quiz items tutored.



Accuracy of tutoring

- Did students passing S1 and S2 students tutor their SimStudents more accurately?



Accuracy of tutoring

- Did students passing S1 and S2 students tutor their SimStudents more accurately?

- Yes!
 - Accuracy of tutoring is a key for success!
- Why were some students more accurate?



Prior knowledge

- Was there a correlation between prior knowledge and accuracy of tutoring?



Prior knowledge

- Was there a correlation between prior knowledge and accuracy of tutoring?

- Yes!
 - US students had higher pre-test scores and tutored more accurately



Prior knowledge

- In the PH
 - There was no diff in prior knowledge between passing and failing S1 students,
 - There was a difference in accuracy of tutoring
 - Weak trend in on the average normalized gain from pre- to post- in favor of passing students
- Passing S1 students learned more



Learning strategy and resource usage

- Did passing S1 students tutor more problems?



Learning strategy and resource usage

- Did passing S1 students tutor more problems?

- No.



Learning strategy and resource usage

- Did passing S1 students refer to more examples?



Learning strategy and resource usage

- Did passing S1 students refer to more examples?
- On average, yes, but this was not statistically confirmed.



Learning strategy and resource usage

- Did passing S1 students copy more example problems for tutoring?



Learning strategy and resource usage

- Did passing S1 students copy more example problems for tutoring?
- Yes!
 - PH students were switching probably copying the worked out examples line-by-line



What did we learn?

- Learning by teaching is tricky.
- Self-explanations can help...a bit.
- Prior knowledge matters...a lot.
- Accuracy of tutoring matters.
- Copying worked-out examples can help.



How did we learn all this?

- SimStudent and similar environments allow us access to fine-grained process data
- Enables deep analysis of student behaviors
- Provides empirical evidence to support or refute theory.



More thanks

- Marc Lester Armenta
- Regina Ira Antonette M. Geli
- Gabriel Jose G. Vitug



And thank **you**!

- Any questions?

